

# Quantifying the measurement errors in a portable open gas-exchange system and their effects on the parameterization of Farquhar *et al.* model for C<sub>3</sub> leaves

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## Abstract

A portable open gas-exchange system (*Li-6400*, *Li-Cor, Inc.*, Lincoln, NE, USA) has been widely used for the measurement of net gas exchanges and calibration/parameterization of leaf models. Measurement errors due to diffusive leakage rates of water vapor ( $L_W$ ) and CO<sub>2</sub> ( $L_C$ ) between inside and outside of the leaf chamber, and the inward dark transpiration rate ( $D_W$ ) and dark respiration rate ( $D_C$ ) released from the leaf under the gasket, can be significant. Rigorous model-based approaches were developed for estimating leakage coefficients of water vapor ( $K_W$ ) and CO<sub>2</sub> ( $K_C$ ) and correcting for the combination of these errors. Models were based on mass balance equations and the Dusty Gas Model for a ternary gas mixture of water vapor, CO<sub>2</sub>, and dry air. Experiments were conducted using two *Li-6400* systems with potato and soybean leaves. Results indicated that models were reliable for estimating  $K_W$  and  $K_C$ , and the values varied with instrument, chamber size, gasket condition, and leaf structure. A thermally killed leaf should be used for this determination. Measurement error effects on parameterization of the Farquhar *et al.* (1980) model as determined by  $P_N/C_i$  curves were substantial and each parameter had its own sensitivity to measurement errors. Results also indicated that all four error sources should be accounted for when correcting measurements.

*Additional key words:* open gas-exchange system; measurement errors; parameterization; leaf model; photosynthesis; transpiration.

## Introduction

Portable open gas-exchange analysis systems with leaf chambers (e.g., *LI-6400*, *Li-Cor, Inc.*, Lincoln, NE, USA) have been widely used for the measurement of net exchange rate of H<sub>2</sub>O ( $E$ ) and CO<sub>2</sub> ( $P_N$ ), the response of  $P_N$  to environment and intercellular CO<sub>2</sub> mole fraction ( $C_i$ ), and calibration and parameterization of leaf models

of  $E$ ,  $P_N$ , and stomatal conductance ( $g_s$ ). The open gas system is a device in which there is a net air flow through the system. Typical open system consists of four major parts: (1) an air supply unit, where air humidity, CO<sub>2</sub> concentration, temperature, *etc.* can be established by some means prior to entering the cuvette, (2) a flow meter

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**Abbreviations:**  $\overline{A_{as}}$  – mean mole fraction of dry air;  $C$  – CO<sub>2</sub> concentration;  $C_a$  – ambient air CO<sub>2</sub> mole fraction;  $C_{AM}$  – total air mixture concentration;  $C_i$  – intercellular CO<sub>2</sub> mole fraction;  $C_r$  – reference CO<sub>2</sub> mole fraction;  $C_s$  – sample CO<sub>2</sub> mole fraction;  $\overline{C_{as}}$  – mean CO<sub>2</sub> mole fraction; DGM – Dusty Gas Model;  $D_{wa}$  – binary diffusivity for water and air;  $D_{cw}$  – binary diffusivity for water and CO<sub>2</sub>;  $D_{ac}$  – binary diffusivity for CO<sub>2</sub> and air;  $D_W^k$  – Knudsen diffusivity for CO<sub>2</sub>;  $D_W^k$  – Knudsen diffusivity for water;  $D_C$  – rate of dark respiration escape from the leaf under gasket;  $D_W$  – rate of dark transpiration escape from the leaf under gasket;  $E$  – water vapor exchange rate;  $E_A$  – apparent water vapor exchange rate;  $E_D$  – dark water vapor exchange rate;  $E_{DA}$  – apparent dark water vapor exchange rate;  $F_i$  – incoming air mole flow rate;  $F_o$  – outgoing air mole flow rate;  $g_b$  – boundary layer conductance for H<sub>2</sub>O;  $g_s$  – stomatal conductance for water vapor; IRGA – infrared gas analyzer;  $J_{max}$  – maximum rate of electron transport;  $K_C$  – diffusion leakage coefficient of CO<sub>2</sub>;  $K_W$  – diffusion leakage coefficient of H<sub>2</sub>O;  $L_A$  – diffusion leakage rate of dry air;  $L_C$  – diffusion leakage rate of CO<sub>2</sub>;  $L_W$  – diffusion leakage rate of water;  $n_{CO_2}$  – number of moles of CO<sub>2</sub>;  $n_{da}$  – number of moles of dry air;  $N_{H_2O}$  – number of moles of water vapor;  $P_{am}$  – pressure of the air mixture;  $P_N$  – net CO<sub>2</sub> exchange rate;  $P_{NA}$  – apparent net CO<sub>2</sub> exchange rate;  $r$  – ratio of inward gas exchange to total gas exchange of the leaf under gasket;  $R$  – universal gas constant;  $R_D$  – dark respiration rate;  $R_{DA}$  – apparent dark respiration rate;  $R_L$  – respiration in the light rate;  $S$  – window area of leaf chamber;  $T$  – temperature of the leaf chamber; TPU – rate of use of triose phosphates;  $V$  – volume of the leaf chamber;  $V_{cmax}$  – maximum rate of Rubisco activity-limited carboxylation;  $W$  – water vapor concentration;  $W_a$  – ambient water vapor mole fraction;  $W_r$  – reference water vapor mole fraction;  $W_s$  – sample water vapor mole fraction;  $\overline{W_{as}}$  – mean mole fraction of water;  $\Delta l$  – diffusion effective length.

for precisely measured incoming air flow rate ( $F_i$ ), (3) a leaf chamber, usually a clamp-on type with four gaskets: two adhered to the upper and lower part of the leaf chamber clamped onto a living leaf, and two air seal gaskets located behind the chamber gaskets, and (4) the infrared gas analyzers (IRGA) for measuring water vapor and  $\text{CO}_2$  mole fraction in the incoming air flow ( $W_r$  and  $C_r$ ) and outgoing air flow ( $W_s$  and  $C_s$ ). Air from the air supply is split into two air flows: one to the reference cell of IRGA, another one, measured by the air flow meter through the leaf chamber, to the analysis cell of IRGA. The measurements are based on the differences in  $\text{H}_2\text{O}$  and  $\text{CO}_2$  between incoming air flow and outgoing flow.

In practice, when the measurements are performed, two groups of measurement errors will inevitably occur to alter the real  $E$  and  $P_N$ . One group includes the diffusive leakage rates of  $\text{H}_2\text{O}$  ( $L_W$ ) and  $\text{CO}_2$  ( $L_C$ ) through the air pathway from the air flow meter to the sample cell of IRGA, *i.e.* through chamber foam gaskets (Long and Hällgren 1993) and the air seal gaskets, air pores between gaskets (or between leaf and gasket if a leaf enclosed) (Flexas *et al.* 2007, Rodeghiero *et al.* 2007), O-rings and other materials (that are not glass or metal) (Li-Cor 2008). Another group includes the effects of inward dark transpiration ( $E_D$ ) and dark respiration ( $R_D$ ) released by the leaf portion under the gasket (Pons and Welschen 2002). The leakages are especially significant when large  $\text{H}_2\text{O}$  and  $\text{CO}_2$  gradients are established between inside and outside the leaf chamber (*e.g.*, the response of  $P_N$  at the lower and higher values of  $C_i$  during measurement of  $P_N/C_i$  curves), or when  $E$  and  $P_N$  are small (*e.g.*, the plant is under environmental stress). Unfortunately, attempts to eliminate or minimize leakages are difficult and have largely failed (Flexas *et al.* 2007). As a result, these measurement errors are often ignored (Pons and Welschen 2002) and it has been incorrectly argued that leakages are not a significant problem with open systems because the chamber is slightly pressured (McDermitt *et al.* 2001, Li-Cor 2008). Long and Hällgren (1993), Long and Bernacchi (2003), McDermitt *et al.* (2001), Bernacchi *et al.* (2001), Flexas *et al.* (2007), Rodeghiero *et al.* (2007), and Li-Cor (2008) have attempted to estimate  $L_C$  and its effects on measurements in the open gas-exchange system. These results demonstrated the significance of  $L_C$  and its substantial effect on  $P_N/C_i$  curves, and/or parameterization of Farquhar *et al.* (1980) model.

However, each of these methods were based on theoretically incomplete approaches and leakage correction results were inconsistent. Li-Cor (2008) and McDermitt *et al.* (2001) used an empty chamber to estimate  $\text{CO}_2$  leakage coefficient ( $K_C$ ) and corrected apparent photosynthesis rate ( $P_{NA}$ ) by directly subtracting  $L_C$  from  $P_{NA}$ . Long and Bernacchi (2003) argued the leakage was increased if a leaf was enclosed within a leaf chamber, and suggested that using a dried leaf to estimate the leakage coefficient at each  $\text{CO}_2$  concentration should be used in correction of  $P_N/C_i$  response. Flexas *et al.* (2007)

stated that the structure of a thermally killed leaf was closer to a living leaf than the dried leaf and observed a substantially lower  $K_C$  with a thermally killed leaf as compared to an empty chamber. They corrected  $P_{NA}$  by simple subtraction of the relationship between  $C_s$  and  $P_{NA}$ . Flexas *et al.* (2007) also concluded that  $L_C$  resulted in an increase up to 40% for day respiration ( $R_L$ ) and a 10% overestimation of the maximum capacity for carboxylation ( $V_{cmax}$ ); however, this error generally did not significantly affect the maximum capacity for electron transport rate ( $J_{max}$ ). However, none of the studies mentioned above incorporated the effects of  $L_W$ ,  $E_D$ , and  $R_D$  on  $P_N$  and  $g_s$ .

Based on the combination of Fick's law and mass balances, Rodeghiero *et al.* (2007) derived different equations for calculation of  $K_C$  and the  $\text{H}_2\text{O}$  leakage coefficient ( $K_W$ ) for an empty chamber and a chamber with a dried leaf, and correction expressions for both apparent transpiration ( $E_A$ ) and  $P_{NA}$ . Their study was the only study to determine  $K_W$  and the effect of  $L_W$  on  $L_C$ . Their observations suggested that  $K_C$  increased, and a  $K_W$  determination was more variable, if a dried leaf was used, and thus empty leaf chamber estimates of  $K_C$  and  $K_W$  could not be used to correct  $E_A$  and  $P_{NA}$ . They also stated that the effect of  $K_W$  on  $K_C$  increased with increasing  $C_s$  up to 60% at  $C_s$  of  $2,000 \mu\text{mol mol}^{-1}$ . Their sensitivity analysis showed that  $L_C$  would overestimate parameters of Farquhar *et al.* (1980) model in the order of  $V_{cmax} < J_{max} < R_L$ . The  $L_W$  further enhanced the overestimation of the model parameters. They observed the effects  $L_W$  on  $P_N/C_i$  curves that were at least as much as  $\text{CO}_2$  diffusion. However, their study did not consider the effects of inward  $E_D$  and  $R_D$  produced by the leaf under the gasket.

Calculations of  $E_A$  and  $P_{NA}$  assume that these gas-exchange processes only occur in the portion of leaf filled in the leaf chamber (Li-Cor 2008). However,  $E_D$  and  $R_D$  from the portion of the leaf under the gasket continue after the leaf is clamped and  $\text{H}_2\text{O}$  and  $\text{CO}_2$  may continually enter the chamber to alter  $W_s$  and  $C_s$ , and outgoing air flow rate ( $F_o$ ) leading to substantial measurement errors, especially when  $E$  and  $P_N$  are low. The pathway for these gasses is mainly along the interface between the gasket and leaf surface but to a lesser extent includes leakage through the leaf mesophyll and gasket itself (Jahnke and Krewitt 2002, Pons and Welschen 2002, Flexas *et al.* 2007). Pons and Welschen (2002) observed an overestimation of  $R_D$  by 55%, exactly the ratio of the inward gasket area to the area of leaf chamber (their estimation of this area ratio was inaccurately computed as 59%), as a result of the rate of dark respiration contributed from the portion of the leaf clamped under the gaskets to the interior of the leaf chamber ( $D_C$ ). The effect of inward  $E_D$  ( $D_W$ ) has not been studied so far.

Neither of the investigations mentioned above were theoretically correct. The problems were not only a result of their incomplete consideration for two groups of errors, but also due to their calculations of  $K_C$  and  $K_W$

from the chamber clamped on a dead leaf (dried or thermally killed leaf), and the correction methods for these measurement errors. They did not take the air leakage rate ( $L_A$ ) into account in their mass balance equation and their leakage equations were derived based on Fick's law. However, Fick's law is valid strictly for isothermal, isobaric and equimolar countercurrent diffusion of a binary gas mixture. Unlike Fick's law, which is empirical, the Dusty Gas Model (DGM) is based on the Chapman Enskog kinetic theory of gases. The DGM is a fundamental approach to gas diffusion in the porous media (Mason and Malinauskas 1983). The DGM includes the Stefan-Maxwell formulation and takes into account Knudsen diffusion. It treats the porous medium as a component of the gas mixture, consisting of giant molecules, like dust in a gas. The DGM can be adapted to

## Materials and methods

**Model description:** Since there are the  $H_2O$  and  $CO_2$  mole gradients between inside and outside the leaf chamber, and inward  $E_D$  and  $R_D$  from the portion of leaf under the gasket,  $H_2O$  and  $CO_2$  must enter or escape the leaf chamber. In the following sections we provide working equations to determine these leakages and to correct the measurement. The detailed derivation of all equations is given in the Appendix and a list of symbols is provided in Table 1.

(1) Diffusive leakage coefficients of an empty chamber

At steady-state condition, the working equations for  $K_W$  and  $K_C$  of an empty chamber are:

$$K_W = \frac{F_i (W_s - W_r)}{(W_a - W_s)} \quad (1)$$

and

$$K_C = \frac{F_i (C_r - C_s)}{(C_s - C_a)} \quad (2)$$

(2) Leakage coefficients of the chamber with a dead leaf

Because a very dry leaf might be a sink of water vapor and a wet leaf could be a source of water vapor, the leakage coefficient of water should be determined when leaf water is balanced with the ambient air. Under this condition, the leakage coefficient of water vapor can be given by Eq. 1. The working equation for estimating leakage of  $CO_2$  is:

$$K_C = \frac{100 P_{NA} S - \frac{K_W (W_s - W_a) C_s}{1000 - W_s}}{C_s - C_a} \quad (3)$$

(3) Correction for the measurement errors

The working equations for correction of the measurement errors for water vapor and  $CO_2$  leakages are:

$$E = E_A + \frac{10 K_W (W_s - W_a)}{S (1000 - W_s)} - r E_D \quad (4)$$

more accurately describe the leakages of  $H_2O$  and  $CO_2$  through the leaf chamber.

In order to obtain the accurate measurements and modeling of gas exchanges of  $H_2O$  and  $CO_2$ , it is necessary to estimate  $K_W$  and  $K_C$ , and  $D_W$  and  $D_C$ , and their effects for any particular leaf under any particular experimental conditions. Quantifying and modeling such effects are needed to revise the existing correction approaches for measurement errors. The objectives of this study are (1) to outline more rigorous model-based approaches for estimating leakage coefficients using the DGM and mass balance equations, (2) to develop methods for correcting  $H_2O$  and  $CO_2$  exchange rates, (3) to estimate the effects of these measurement errors on the parameterization of the  $C_3$  leaf model of Farquhar *et al.* (1980).

and

$$P_N = P_{NA} - \frac{K_W (W_s - W_a) C_s}{100 S (1000 - W_s)} + \frac{K_C (C_a - C_s)}{100 S} - r R_D \quad (5)$$

(4) Calculation of  $g_s$  and  $C_i$

Because of the correction of the measurement errors,  $g_s$  and  $C_i$  have to be recalculated according to corrected  $E$  and  $P_N$ . In this paper, we treat only two particular cases: the hypostomatous leaf where only one side of the leaf has stomata, and the symmetrical amphistomatous leaf where physiological and environmental conditions are identical in both leaf sides, *i.e.*  $W_i$  and  $W_a$ ,  $C_i$  and  $C_a$ , stomatal conductance for water vapor ( $g_s$ ) and boundary layer conductance ( $g_b$ ) are the same. Following von Caemmerer and Farquhar (1981), for hypostomatous leaf,  $g_s$  can be estimated by:

$$g_s = \frac{\left(1 - \frac{W_i + W_s}{2000}\right) g_b E}{(W_i - W_s) g_b - \left(1 - \frac{W_i + W_s}{2000}\right) E} \quad (6a)$$

$C_i$  is given by

$$C_i = \frac{\left(\frac{g_s g_b}{1.6 g_b + 1.37 g_s} - \frac{E}{2000}\right) C_s - P_N n}{\frac{g_s g_b}{1.6 g_b + 1.37 g_s} + \frac{E}{2000}} \quad (7a)$$

where 1.6 and 1.37 are the ratio of the stomatal conductance to  $H_2O$  and to  $CO_2$  in air and in the boundary layer, respectively. For the symmetrical amphistomatous leaf,  $g_s$  and  $C_i$  are given respectively by:

$$g_s = \frac{\left(1 - \frac{W_i + W_s}{2000}\right) g_b E}{2 (W_i - W_s) g_b - \left(1 - \frac{W_i + W_s}{2000}\right) E} \quad (6b)$$

and

$$C_i = \frac{\left(\frac{g_s (2 g_b)}{1.6 (2 g_b) + 1.37 g_s} - \frac{E}{2000}\right) C_s - P_N}{\frac{g_s (2 g_b)}{1.6 (2 g_b) + 1.37 g_s} + \frac{E}{2000}} \quad (7b)$$

Table 1. List of model variables and their units.

| Variable            | Definition  | Unit  |
|---------------------|---|---|
| $\overline{A}_{as}$ | Mean mole fraction of dry air   | [mmol(air) mol <sup>-1</sup> ]                                  |
| $P_N$               | Net CO <sub>2</sub> exchange rate   | [ $\mu$ mol(CO <sub>2</sub> ) m <sup>-2</sup> s <sup>-1</sup> ] |
| $P_{NA}$            | Apparent net CO <sub>2</sub> exchange rate                                  | [ $\mu$ mol(CO <sub>2</sub> ) m <sup>-2</sup> s <sup>-1</sup> ] |
| $C$                 | CO <sub>2</sub> concentration   | [mol(CO <sub>2</sub> ) m <sup>-3</sup> ]                        |
| $C_a$               | Ambient air CO <sub>2</sub> mole fraction                                   | [ $\mu$ mol(CO <sub>2</sub> ) mol <sup>-1</sup> (air)]          |
| $C_{AM}$            | Total air mixture concentration   | [mol m <sup>-3</sup> ]  |
| $C_i$               | Intercellular CO <sub>2</sub> mole fraction                                 | [ $\mu$ mol(CO <sub>2</sub> ) mol <sup>-1</sup> (air)]          |
| $C_r$               | Reference CO <sub>2</sub> mole fraction                                     | [ $\mu$ mol(CO <sub>2</sub> ) mol <sup>-1</sup> (air)]          |
| $C_s$               | Sample CO <sub>2</sub> mole fraction  | [ $\mu$ mol(CO <sub>2</sub> ) mol <sup>-1</sup> (air)]          |
| $\overline{C}_{as}$ | Mean CO <sub>2</sub> mole fraction  | [ $\mu$ mol(CO <sub>2</sub> ) mol <sup>-1</sup> (air)]          |
| $D_{wa}$            | Binary diffusivity for water and air  | [m <sup>2</sup> s <sup>-1</sup> ]                               |
| $D_{cw}$            | Binary diffusivity for water and CO <sub>2</sub>                            | [m <sup>2</sup> s <sup>-1</sup> ]                               |
| $D_{ac}$            | Binary diffusivity for CO <sub>2</sub> and air                              | [m <sup>2</sup> s <sup>-1</sup> ]                               |
| $D_W^c$             | Knudsen diffusivity for CO <sub>2</sub>                                     | [m <sup>2</sup> s <sup>-1</sup> ]                               |
| $D_W^k$             | Knudsen diffusivity for water   | [m <sup>2</sup> s <sup>-1</sup> ]                               |
| $D_C$               | Rate of dark respiration escape from the leaf under gasket                  | [ $\mu$ mol(CO <sub>2</sub> ) m <sup>-2</sup> s <sup>-1</sup> ] |
| $D_W$               | Rate of dark transpiration escape from the leaf under gasket                | [mmol (CO <sub>2</sub> ) m <sup>-2</sup> s <sup>-1</sup> ]      |
| $E$                 | Water vapor exchange rate   | [mmol(H <sub>2</sub> O) m <sup>-2</sup> s <sup>-1</sup> ]       |
| $E_A$               | Apparent water vapor exchange rate  | [mmol(H <sub>2</sub> O) m <sup>-2</sup> s <sup>-1</sup> ]       |
| $E_D$               | Dark water vapor exchange rate  | [mmol(H <sub>2</sub> O) m <sup>-2</sup> s <sup>-1</sup> ]       |
| $E_{DA}$            | Apparent dark water vapor exchange rate                                     | [mmol(H <sub>2</sub> O) m <sup>-2</sup> s <sup>-1</sup> ]       |
| $F_i$               | Incoming air mole flow rate   | [ $\mu$ mol(air) s <sup>-1</sup> ]                              |
| $F_o$               | Outgoing air mole flow rate   | [ $\mu$ mol(air) s <sup>-1</sup> ]                              |
| $g_b$               | Boundary layer conductance for H <sub>2</sub> O                             | [mol(H <sub>2</sub> O) m <sup>-2</sup> s <sup>-1</sup> ]        |
| $g_s$               | Stomatal conductance for water vapor  | [mol(H <sub>2</sub> O) m <sup>-2</sup> s <sup>-1</sup> ]        |
| $J_{max}$           | Maximum rate of electron transport  | [ $\mu$ mol(e <sup>-</sup> ) m <sup>-2</sup> s <sup>-1</sup> ]  |
| $K_C$               | Diffusion leakage coefficient of CO <sub>2</sub>                            | [ $\mu$ mol(CO <sub>2</sub> ) s <sup>-1</sup> ]                 |
| $K_W$               | Diffusion leakage coefficient of H <sub>2</sub> O                           | [ $\mu$ mol(H <sub>2</sub> O) s <sup>-1</sup> ]                 |
| $L_A$               | Diffusion leakage rate of dry air   | [mmol(air) s <sup>-1</sup> ]                                    |
| $L_C$               | Diffusion leakage rate of CO <sub>2</sub>                                   | [ $\mu$ mol(CO <sub>2</sub> ) s <sup>-1</sup> ]                 |
| $L_W$               | Diffusion leakage rate of water   | [mmol(H <sub>2</sub> O) s <sup>-1</sup> ]                       |
| $n_{CO_2}$          | Number of moles of CO <sub>2</sub>  |   |
| $n_{da}$            | Number of moles of dry air  |   |
| $N_{H_2O}$          | Number of moles of water vapor  |   |
| $P_{am}$            | Pressure of the air mixture   | [Pa]  |
| $r$                 | Ratio of inward gas exchange to total gas exchange of the leaf under gasket |   |
| $R$                 | Universal gas constant  | 8.314 J mol <sup>-1</sup> K <sup>-1</sup>                       |
| $R_D$               | Dark respiration rate   | [ $\mu$ mol(CO <sub>2</sub> ) m <sup>-2</sup> s <sup>-1</sup> ] |
| $R_{DA}$            | Apparent dark respiration rate  | [ $\mu$ mol(CO <sub>2</sub> ) m <sup>-2</sup> s <sup>-1</sup> ] |
| $R_L$               | Respiration in the light rate   | [ $\mu$ mol(CO <sub>2</sub> ) m <sup>-2</sup> s <sup>-1</sup> ] |
| $S$                 | Window area of leaf chamber   | [cm <sup>-2</sup> ]   |
| $T$                 | Temperature of the leaf chamber   | [K]   |
| $TPU$               | Rate of use of triose phosphates  | [ $\mu$ mol(CO <sub>2</sub> ) m <sup>-2</sup> s <sup>-1</sup> ] |
| $V$                 | Volume of the leaf chamber  | [m <sup>3</sup> ]   |
| $V_{cmax}$          | Maximum rate of Rubisco activity-limited carboxylation                      | [ $\mu$ mol(CO <sub>2</sub> ) m <sup>-2</sup> s <sup>-1</sup> ] |
| $W$                 | Water vapor concentration   | [mol(H <sub>2</sub> O) m <sup>-3</sup> (air)]                   |
| $W_a$               | Ambinet water vapor mole fraction   | [mmol(H <sub>2</sub> O) mol <sup>-1</sup> (air)]                |
| $W_r$               | Reference water vapor mole fraction   | [mmol(H <sub>2</sub> O) mol <sup>-1</sup> (air)]                |
| $W_s$               | Sample water vapor mole fraction  | [mmol(H <sub>2</sub> O) mol <sup>-1</sup> (air)]                |
| $\overline{W}_{as}$ | Mean mole fraction of water   | [mmol(H <sub>2</sub> O) mol <sup>-1</sup> (air)]                |
| $\Delta l$          | Diffusion effective length  | [m]   |

Eq. 6b is very similar to Eq. 6a, except that the factor 2 arises in the first term of the denominator as a result of use of  $g_s$  defined on a single surface area basis for symmetrical amphistomatous leaf. The magnitude  $g_s$  from Eq. 6b is half of the corresponding value estimated by

equation provided by *Li-Cor* (2008), where  $g_s$  was defined as combined conductance for stomatal conductance in both sides of the leaf. (Mention of a trademark or proprietary product does not constitute a guarantee or warranty of the product by the USDA and does not

imply the exclusion of other available products.)

(5) Calculation of parameters of photosynthesis biochemical model

After correction of  $P_N/C_i$  curves, the parameters of the Farquhar *et al.* (1980) model for  $C_3$  plant, the maximum velocity of Rubisco for carboxylation ( $V_{cmax}$ ), the maximum rate of electron transport ( $J_{max}$ ); the rate of use of triose phosphates (TPU) and the respiratory  $CO_2$  release other than by photorespiration (primarily mitochondrial respiration) ( $R_L$ ), were estimated by fitting method as suggested by Sharkey *et al.* (2007).

**Plant materials:** Two  $C_3$  plants, potato (*Solanum tuberosum* L. cv. Kennebec) with hypostomatous leaves (Pachepsky and Acock 1998), and soybean (*Glycine max* Merr. cv. Kent), with amphistomatous leaves (Bunce 2006), were used for the experiments. Potato plants were grown in 16-L pots with a 3:1 mixture of sand:vermiculite and soybeans in 2-L pots with vermiculite. Pots were fertigated until free drainage from the bottom of the pot daily using half-strength Woody's solution (Robinson 1984). Soybeans were initially grown in controlled environment chambers at a  $1,000 \mu\text{mol m}^{-2} \text{s}^{-1}$  photosynthetic photon flux density (PPFD) for 12 h per day ( $43.2 \text{ mol PAR m}^{-2} \text{d}^{-1}$ ), with constant air temperature of  $25^\circ\text{C}$ . Following reproductive stage R3, soybeans were moved to an outdoor pad where conditions averaged  $44.2 \pm 17 \text{ mol PAR m}^{-2} \text{d}^{-1}$ ,  $18.7 \pm 4.8^\circ\text{C}$ , and relative humidity ranged between 50 and 100% for the remainder of the study. Potatoes were grown on the same outdoor pad where conditions averaged  $44.1 \pm 15.8 \text{ mol PAR m}^{-2} \text{d}^{-1}$ ,  $16.2 \pm 5.3^\circ\text{C}$ , and relative humidity ranged between 45 and 100%. These were typical conditions for the months of April, May, and June in Beltsville, MD, USA. Soybeans were at the R3 stage during measurements and potatoes were approximately 21 days post tuber initiation. Mature, fully green leaves within seven days of achieving full expansion were used for leaf measurements for both plants (second and third trifoliate leaves for soybeans and fourth or fifth leaf from top of the canopy for potato).

For homobaric leaves with significant lateral gas exchange (Jahnke 2001, Jahnke and Krewitt 2002, Pieruschka *et al.* 2005, 2006), determination of the ratio of inward gas exchange to the total gas exchange of the leaf under gasket is difficult. However, Flexas *et al.* (2007) and Morison and Lawson (2007) argued that the lateral diffusion was much smaller than the leakage between the leaf and gasket surface. In this study, for simplification, we assumed both potato and soybean leaves were heterobaric leaves.

**Determining  $H_2O$  and  $CO_2$  leakage coefficients:** The experiments were conducted in the laboratory using two Li-6400 systems equipped with either a  $2 \text{ cm}^2$  fluorometer head model 6400-40 or a  $6 \text{ cm}^2$  head 6400-02B (Li-Cor, Inc., Lincoln, NE, USA). One was used for gas-

exchange measurements and another was used for monitoring the ambient air mole fractions of water vapor and  $CO_2$  in the immediate vicinity of the leaf chamber. Instruments were marked as instrument-A and -B. Before measurements, the two instruments were calibrated for  $CO_2$  using standard gases with  $CO_2$  mole fraction of 0, 361, 727, and  $1,004 \mu\text{mol mol}^{-1}$  according to the procedure suggested by the manufacturer (Li-Cor 2008). For the water vapor calibration, the  $H_2O$  zero of instrument IRGAs were checked daily using chemical methods as suggested by the manufacturer (Li-Cor 2008). Both instruments were initially compared against one another with respect to the same ambient air and measured water vapor readings were less than  $0.3 \text{ mmol mol}^{-1}$ . The lower gasket of both leaf chambers was made of black neoprene foam, the upper white gasket was made of white polyethylene foam as provided by the manufacturer.

The leakage coefficients in instrument-B with a worn gasket (which had been previously used for at least 40 h) were obtained by three series of measurements. These included (1) an empty chamber, (2) chamber clamped on a dried leaf, or (3) chamber clamped on a thermally killed leaf. The block temperature was set to  $25\text{--}30^\circ\text{C}$  similar to the ambient air temperature. Note that the leakage coefficients vary with the 1.5 to 1.8 power of temperature (Cussler 2007), but at this temperature range, the effects are very small, about 3%. At each measurement, we waited until steady-state conditions were observed, then the IRGAs were matched before recording the data. Each measurement was replicated at least three times. To get large water vapor and  $CO_2$  gradients for estimating  $K_C$  and  $K_W$ ,  $CO_2$ -response curves were performed under different water vapor gradient conditions. These curves were obtained using two different leaf chambers:  $2 \text{ and } 6 \text{ cm}^2$ . During these measurements, external ambient  $CO_2$  concentration varied between 385 and  $560 \mu\text{mol mol}^{-1}$  and ambient water vapor varied between 10 and  $25 \text{ mmol mol}^{-1}$ .

To compare the leakage coefficient difference between the two instruments, additional experiments were conducted in instrument-A with or without a dead leaf filled in the  $6 \text{ cm}^2$  leaf chamber. The differences of leakage coefficients for different gasket wear conditions were examined by an additional experiment conducted using new gaskets with a thermally killed leaf inside the  $6 \text{ cm}^2$  chamber. To examine the possible effect of leaf thickness on  $K_C$  as noted by Flexas *et al.* (2007), we rehydrated a dried leaf with distilled water for 2 h to make the leaf thicker and the structure closer to a living leaf. This effect was measured by the measurements with the dried leaf vs. the rehydrated leaf.

**Determining the gas exchanges of potato and soybean leaves:** The results reported in the following sections were estimated using instrument-B with worn gaskets unless otherwise noted. To get the desired water vapor gradient, when water vapor mole fraction in ambient air was high, the valve of the desiccant tube was adjusted to

decrease the water vapor mole fraction inside the chamber for negative gradients of  $-25$  and  $-15$   $\text{mmol mol}^{-1}$ ; and when ambient water vapor mole fraction was low, a few drops of distilled water were added to the soda lime tube to increase water vapor mole fraction inside the chamber in order to get the desired gradient of  $15$   $\text{mmol mol}^{-1}$ . The leaf gas exchange was determined using two *Li-6400* instruments with a similar procedure as described already for estimating  $K_W$  and  $K_C$ . The measurements were made on the youngest fully expanded leaves. The  $E_D$  and  $R_D$  rates of potato and soybean were measured using the  $6\text{ cm}^2$  chamber. After achieving the steady state, the IRGA's were matched and data recorded.

To quantify the effects of measurement errors induced by  $L_W$  and  $L_C$ , and  $D_W$  and  $D_C$  on parameterization of the Farquhar *et al.* (1980) for  $C_3$  plants,  $P_N/C_i$  curves were

determined in potato and soybean fully expand mature leaves under different  $W_s$ . The leaf temperature was set close to ambient air temperature. The measurements were performed using  $2$  and  $6\text{ cm}^2$  chambers. To obtain large water vapor gradient between inside and outside leaf chamber, the high reference water vapor mole fraction was achieved by adding a few drops of distilled water to the soda lime and the incoming air would be humidified through the bypass valve of the desiccant tube. The high ambient air humidity was achieved by conducting the measurements inside an outdoor sunlit growth chamber (Fleisher *et al.* 2008). The water vapor gradient ranged from  $-15$  to  $+20$   $\text{mmol mol}^{-1}$ . The measurements were replicated at least 3 times at different water vapor gradients using two different size chambers.

## Results

**Leakage coefficients of the empty chamber:** The slopes of linear regression relationships  $F_i(W_s - W_r)$  vs.  $(W_a - W_s)$  (Eq. 1), and  $F_i(C_r - C_s)$  vs.  $(C_s - C_a)$  (Eq. 2) were estimates of  $K_W$  and  $K_C$ , respectively, as shown in Fig. 1 in instrument-B for the worn gasket. Overall,  $K_W$  was  $4.34\text{ }\mu\text{mol s}^{-1}$  in the  $2\text{ cm}^2$  chamber and  $3.60\text{ }\mu\text{mol s}^{-1}$  in the  $6\text{ cm}^2$  chamber,  $K_C$  was  $0.42\text{ }\mu\text{mol s}^{-1}$  in the  $2\text{ cm}^2$  chamber and  $0.46\text{ }\mu\text{mol s}^{-1}$  in the  $6\text{ cm}^2$  chamber. Results for instrument-A with a  $6\text{ cm}^2$  chamber and worn gasket

included a  $K_W$  of  $6.75\text{ }\mu\text{mol s}^{-1}$  and  $K_C$  of  $0.94\text{ }\mu\text{mol s}^{-1}$  (data not shown).

**Effect of presence of a leaf:** Fig. 2 showed two representative examples of changes in calculated  $K_W$  (Eq. 3) vs. time for a dried and a thermally killed potato leaf by instrument-A. When the interior air of the leaf chamber is more humid than the exterior air, a clamped dried potato leaf will absorb  $\text{H}_2\text{O}$  from its environment, resulting

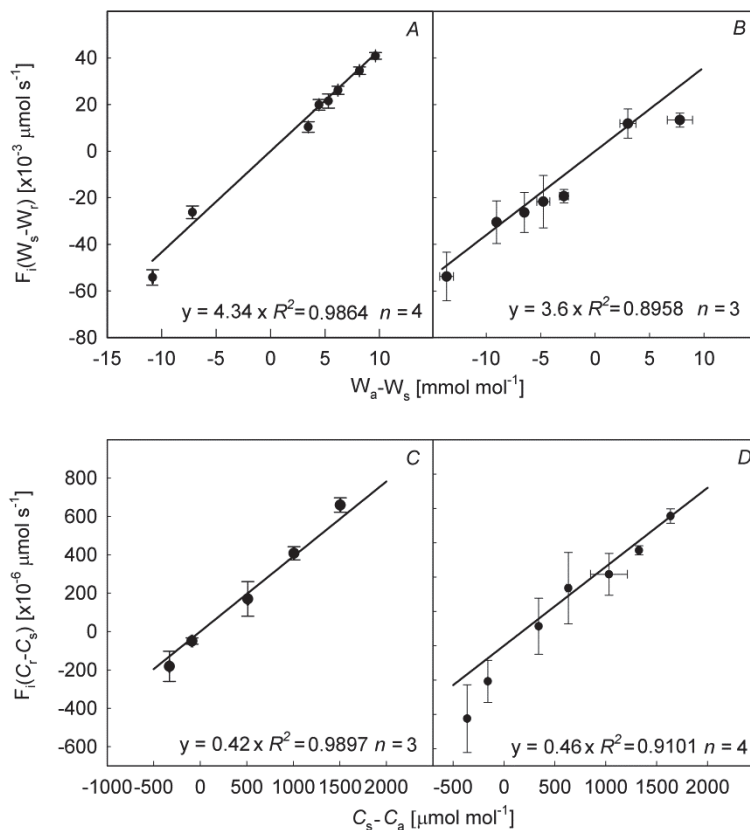


Fig. 1. The response of leakages of water vapor (A, B) and  $\text{CO}_2$  (C, D) to the mole fraction gradients between inside and outside an empty chamber in instrument-B fitted with a worn gasket. Graphs A and C showed results for the  $2\text{ cm}^2$  chamber, and B and D the  $6\text{ cm}^2$  chamber. Values are the mean  $\pm$  SD ( $n = 3$  or  $4$ ).

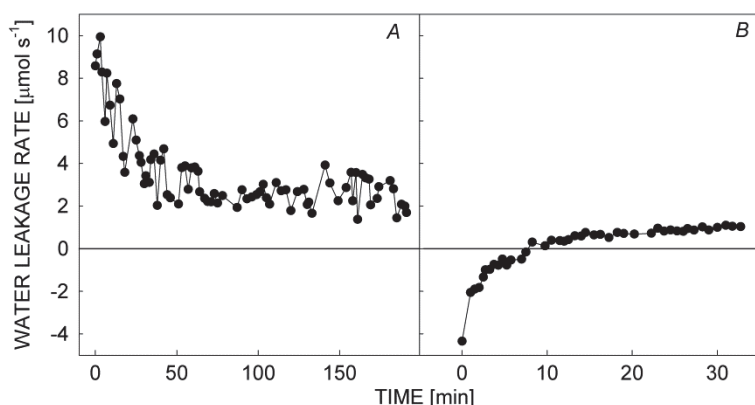


Fig. 2. Changes in calculated water vapor leakage coefficient with time for instrument-A. The chamber size was 6 cm<sup>2</sup> with worn gaskets. A dried potato leaf was used inside a more humid leaf chamber in graph A, and a thermally killed one inside a drier leaf chamber in graph B. Data are shown for a single leaf as an illustration.

Table 2. Leakage coefficients of water ( $K_W$ ) and CO<sub>2</sub> ( $K_C$ ) for a dead leaf (thermally killed leaf or dried leaf) determined by instrument-A or -B with worn gaskets. The  $K_W$  was determined as the slope of regression when the leaf water was balanced with ambient air. The values of  $K_W$  were means  $\pm$  SD. The values of  $K_C$  were the slope of linear regression relationship  $100 P_{NA} S - \frac{K_W(W_s - W_a) C_s}{1000 - W_s}$  vs.  $(C_s - C_a)$  (Eq. 21a) followed by correlation coefficients ( $n = 3$ ). <sup>a</sup> – thermally killed leaf with worn gaskets; <sup>b</sup> – dried leaf with worn gaskets; <sup>c</sup> – dried leaf (rehydrated) with worn gaskets, the values of the first line were obtained when the leaf was wet, while the values of the second line were obtained after the leaf was dried; <sup>d</sup> – thermally killed leaf with new gaskets.

| Instrument |                                  | Chamber area<br>[cm <sup>2</sup> ] | Plant               |                      |                                |
|------------|----------------------------------|------------------------------------|---------------------|----------------------|--------------------------------|
| -A         | $K_W$ [ $\mu\text{mol s}^{-1}$ ] | 6                                  | Potato <sup>a</sup> | Potato <sup>b</sup>  | Potato <sup>c</sup>            |
|            |                                  |                                    | 0.72 $\pm$ 0.03     | 1.11 $\pm$ 0.05      |                                |
|            |                                  |                                    | 1.06 $\pm$ 0.03     | 1.84 $\pm$ 0.14      |                                |
|            | $K_C$ [ $\mu\text{mol s}^{-1}$ ] | 6                                  | 1.60 $\pm$ 0.05     | 2.71 $\pm$ 0.04      |                                |
|            |                                  |                                    | 0.82 (0.9592)       | 0.96 (0.9724)        | 0.92 (0.9702)<br>0.88 (0.9644) |
| -B         | $K_W$ [ $\mu\text{mol s}^{-1}$ ] | 2                                  | Potato <sup>a</sup> | Soybean <sup>a</sup> | Potato <sup>d</sup>            |
|            |                                  |                                    | 0.44 $\pm$ 0.00     | 0.52 $\pm$ 0.03      |                                |
|            |                                  |                                    | 0.73 $\pm$ 0.08     | 0.62 $\pm$ 0.07      |                                |
|            |                                  | 6                                  | 1.14 $\pm$ 0.03     | 1.52 $\pm$ 0.02      |                                |
|            |                                  |                                    | 1.49 $\pm$ 0.03     | 0.39 $\pm$ 0.03      | 0.75 $\pm$ 0.03                |
|            | $K_C$ [ $\mu\text{mol s}^{-1}$ ] | 2                                  | 2.36 $\pm$ 0.47     | 1.45 $\pm$ 0.01      | 1.06 $\pm$ 0.09                |
|            |                                  |                                    | 3.38 $\pm$ 0.24     | 2.24 $\pm$ 0.06      | 1.76 $\pm$ 0.09                |
|            |                                  |                                    | 0.43 (0.9273)       | 0.49 (0.9085)        |                                |
|            |                                  | 6                                  | 0.89 (0.9587)       | 0.58 (0.9794)        | 0.56 (0.9047)                  |

initially in a more negative  $E_A$  and a higher  $K_W$ . The  $K_W$  then decreased to a relatively constant value of 2.0  $\mu\text{mol s}^{-1}$  after about 50 min (Fig. 2A) (Note that relative humidity was less than 75% to avoid condensing of water within the interior of the air sample lines). Fig. 2B showed the changes in calculated  $K_W$  of a thermally killed leaf with time. In contrast with the dried leaf results, the water vapor that evaporated from the wet leaf inside the leaf chamber made a larger positive  $E_A$ , as this evaporated water vapor was much larger than leakage to the exterior chamber at beginning of the measurement. This larger positive  $E_A$  made a negative  $K_W$ . As evaporation decreased with time the leaf was balanced with surrounding air (after about 20 min),  $K_W$  became positive and stabilized at ca. 1.0  $\mu\text{mol s}^{-1}$ .

Table 2 showed  $K_W$  and  $K_C$  with a dead leaf determined by instrument-A or -B under different conditions. Overall,  $K_W$  was consistent for a given leaf.

However, it varied between species and amongst individual leaves of the same species in different chambers with different gasket conditions. The range of  $K_W$  of the same species was large. For example, for soybean leaves,  $K_W$  ranged from 0.39 to 2.24  $\mu\text{mol s}^{-1}$  for the 6 cm<sup>2</sup> chamber with worn gaskets. The  $K_W$  with a dead leaf was much less than that of the empty chamber.

$K_C$  was estimated by Eq. 3 as the linear regression slope of  $100 P_{NA} S - \frac{K_W(W_s - W_a) C_s}{1000 - W}$  vs.  $(C_a - C_s)$ .

Overall  $K_C$  was stable for different leaves from the same species in a specific chamber as shown in Table 2 for the dead leaves determined by both instrument-A or -B with differently sized chamber and different gaskets. In general,  $K_C$  of 2 cm<sup>2</sup> chamber was less than that of 6 cm<sup>2</sup> chamber and  $K_C$  with a dead leaf was similar or greater than that for an empty chamber. As expected,  $K_C$

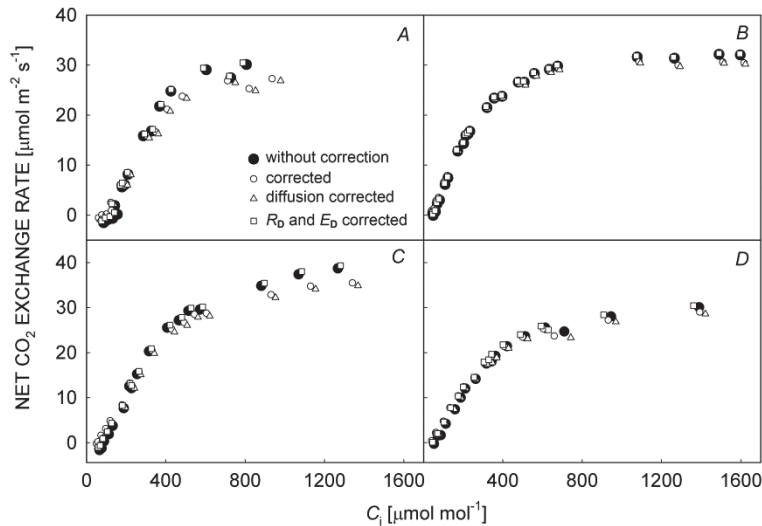


Fig. 3. The net CO<sub>2</sub> exchange rate vs. intercellular CO<sub>2</sub> mole fraction ( $C_i$ ) for potato (A, B) and soybean (C, D) leaves without correction (closed circles), with corrections for both diffusion leakages and inward gas exchanges from leaf under gasket (open circles), corrected for only diffusion leakages (open triangles), and corrected for only inward gas exchanges from leaf under gasket (open squares). The measurements were conducted with the Li-6400-40 leaf chamber (2 cm<sup>2</sup>) (A, C) and Li-6400 2B leaf chamber (6 cm<sup>2</sup>) (B, D).

Table 3. The parameters of Farquhar *et al.* (1980) model estimated by  $P_N/C_i$  curves, corrected with both the leakages and inward gas exchanges under the gasket, without correction, corrected with only the leakages, and corrected with only inward gas exchange from the leaf under the gasket, for two leaf chamber sizes and for potato and soybean leaves. <sup>a</sup> – the value was corrected for both diffusion leakages and inward gas exchange from the leaf portion under the gasket; <sup>b</sup> – the value was corrected for only the diffusion leakages; <sup>c</sup> – the value was corrected for only the inward gas exchange from the leaf portion under the gasket; <sup>d</sup> – CV is the corrected value.

| Plant   | Chamber size [cm <sup>2</sup> ] | Parameter [µmol m <sup>-2</sup> s <sup>-1</sup> ] | Corrected value <sup>a</sup> | Without correction value | Without correction value/CV <sup>d</sup> | Diffusion correction <sup>b</sup> value | Diffusion correction <sup>b</sup> value/CV | Inward dark <sup>c</sup> value | Inward dark <sup>c</sup> value/CV |
|---------|---------------------------------|---|------------------------------|--------------------------|--|---|--|--------------------------------|-----------------------------------|
| potato  | 2                               | $V_{cmax}$  | 80.39                        | 87.54                    | 1.09                                     | 72.67                                   | 0.90                                       | 88.90                          | 1.11                              |
|         |                                 | $J_{max}$   | 100.10                       | 114.31                   | 1.14                                     | 100.85                                  | 1.01                                       | 108.38                         | 1.08                              |
|         |                                 | TPU   | 7.22                         | 9.07                     | 1.26                                     | 7.52                                    | 1.04                                       | 8.69                           | 1.20                              |
|         |                                 | $R_L$   | 1.76                         | 4.73                     | 2.69                                     | 2.68                                    | 1.52                                       | 3.62                           | 2.06                              |
|         | 6                               | $V_{cmax}$  | 129.20                       | 141.01                   | 1.09                                     | 126.23                                  | 0.98                                       | 143.77                         | 1.11                              |
|         |                                 | $J_{max}$   | 121.53                       | 134.74                   | 1.11                                     | 124.23                                  | 1.02                                       | 131.78                         | 1.08                              |
|         |                                 | TPU   | 8.54                         | 9.66                     | 1.13                                     | 8.74                                    | 1.02                                       | 9.46                           | 1.11                              |
|         |                                 | $R_L$   | 0.10                         | 2.38                     | 23.78                                    | 0.87                                    | 8.68                                       | 1.61                           | 16.04                             |
| soybean | 2                               | $V_{cmax}$  | 95.11                        | 105.01                   | 1.10                                     | 90.93                                   | 0.96                                       | 110.93                         | 1.17                              |
|         |                                 | $J_{max}$   | 117.64                       | 141.96                   | 1.21                                     | 122.10                                  | 1.04                                       | 138.18                         | 1.17                              |
|         |                                 | TPU   | 8.98                         | 10.97                    | 1.22                                     | 9.34                                    | 1.04                                       | 10.63                          | 1.18                              |
|         |                                 | $R_L$   | 0.91                         | 4.59                     | 5.04                                     | 2.35                                    | 2.58                                       | 3.22                           | 3.53                              |
|         | 6                               | $V_{cmax}$  | 123.46                       | 101.91                   | 0.83                                     | 89.69                                   | 0.73                                       | 140.79                         | 1.14                              |
|         |                                 | $J_{max}$   | 106.44                       | 119.12                   | 1.12                                     | 106.91                                  | 1.00                                       | 118.69                         | 1.12                              |
|         |                                 | TPU   | 7.93                         | 8.89                     | 1.12                                     | 8.06                                    | 1.02                                       | 8.63                           | 1.09                              |
|         |                                 | $R_L$   | 0.00                         | 2.06                     |  | 0.71                                    |  | 0.95                           |                                   |

of 0.56 µmol s<sup>-1</sup> for 6 cm<sup>2</sup> chamber with new gaskets filled with a thermally killed potato leaf was less than that of 0.89 µmol s<sup>-1</sup> with worn gaskets (Table 2), implying that the worn gasket should be replaced regularly to get less leakage error.

We used instrument-A to compare the effect of leaf structure on  $K_C$  for a 6 cm<sup>2</sup> chamber as  $K_C$  was determined with dried leaves, thermally killed leaves and a rehydrated leaf. The results showed that  $K_C$  of dried leaves was greater than that of the rehydrated leaf which was greater than that of thermally killed leaves (Table 2), and the  $K_C$  difference between dried leaves and thermally killed leaves was 17%, implying that the structure of a dead potato leaf could influence  $K_C$ . Considering the structural similarity of a dead leaf to a living leaf, the

correction of measurement error should be based on the value estimated by a thermally killed leaf. Even  $K_C$  in the 2 cm<sup>2</sup> chamber could be up to two times less than that in the 6 cm<sup>2</sup> chamber with thermally killed leaves for both potato and soybean plants; however, the 2 cm<sup>2</sup> chamber will have larger leakage errors than 6 cm<sup>2</sup> chamber since the leakage error is based on unit area (Eq. A31a).

**Effects on photosynthesis parameterization from  $P_N/C_i$  curves:** To correct the effects of inward gas exchange ( $R_D$  and  $E_D$ ) from the leaf under gasket on measurements,  $R_D$  and  $E_D$  of a leaf have to be determined. Using instrument-B with the 6 cm<sup>2</sup> chamber,  $R_{DA}$  and  $E_{DA}$  were measured with three leaves for each potato and soybean plant. After applying Eq. A24 and Eq. A25,  $R_D$  was



$0.40 \pm 0.10 \mu\text{mol m}^{-2} \text{s}^{-1}$  and  $E_D$  was  $0.08 \pm 0.10 \text{ mmol m}^{-2} \text{s}^{-1}$  for potato leaves.  $R_D$  was  $0.67 \pm 0.32 \mu\text{mol m}^{-2} \text{s}^{-1}$  and  $E_D$  was  $0.14 \pm 0.05 \text{ mmol m}^{-2} \text{s}^{-1}$  for soybean leaves. The large variation of  $R_D$  or  $E_D$  reflected differences among leaves from the same plant, which may reflect varying leaf physiological condition.

The effects of measurement errors from the  $L_W$  and  $L_C$ , and the  $E_D$  and  $R_D$  on  $P_N/C_i$  curves were examined using two chamber sizes and two different plants (Fig. 3). Overall,  $P_N$  corrected for  $E_D$  and  $R_D$ , and  $L_W$  and  $L_C$ , was under-estimated at low  $C_i$  and over-estimated at high  $C_i$ , which was mainly because of the change in the direction of the  $\text{CO}_2$  gradient.  $C_i$  was larger than that estimated by the *Li-6400* before correction. However, if  $P_N$  and  $C_i$  were only corrected for  $E_D$  and  $R_D$  they were closer to the values observed without correction. The measurement errors in the  $6 \text{ cm}^2$  chamber were less than that in  $2 \text{ cm}^2$  chamber. For example, in  $2 \text{ cm}^2$  chamber,  $P_N$  was  $30.4 \mu\text{mol m}^{-2} \text{s}^{-1}$  corresponding to  $32.0 \mu\text{mol m}^{-2} \text{s}^{-1}$  without correction, an overestimation of  $1.6 \mu\text{mol m}^{-2} \text{s}^{-1}$  (Fig. 3C); in  $6 \text{ cm}^2$  chamber, the measurement error was only  $1.1 \mu\text{mol m}^{-2} \text{s}^{-1}$  (Fig. 3D). The relative measurement error was larger at low  $C_i$ . For example, for soybean leaf in  $2 \text{ cm}^2$  chamber, at  $C_i$   $40 \mu\text{mol mol}^{-1}$ , the relative

measurement error could be 176% but at a high  $C_i$  of  $1,400 \mu\text{mol mol}^{-1}$ , the relative error was only about 5% (Fig. 3C).

$V_{\text{cmax}}$ ,  $J_{\text{max}}$ , TPU, and  $R_L$  parameters were estimated with and without correction for only  $E_D$  and  $R_D$ , only  $L_W$  and  $L_C$ , and for all these measurement errors from the  $P_N/C_i$  curves for potato and soybean leaves (Table 3).  $R_L$  was the most sensitive to measurement errors since the  $R_L$  was relative small. For example,  $R_L$  of a soybean leaf determined by the  $2 \text{ cm}^2$  chamber was  $4.95 \mu\text{mol m}^{-2} \text{s}^{-1}$  which overestimated the corrected value by five times (Table 3).  $J_{\text{max}}$  and TPU were overestimated but  $V_{\text{cmax}}$  could be overestimated or underestimated since both  $C_i$  and  $P_N$  were affected not only in magnitude but also by the direction of  $\text{H}_2\text{O}$  and  $\text{CO}_2$  gradients. If only corrected by diffusion leakages,  $V_{\text{cmax}}$  typically declined but  $J_{\text{max}}$  and TPU were enhanced. When only the effects of  $E_D$  and  $R_D$  were included, all parameters increased for soybean leaf in the  $6 \text{ cm}^2$  chamber. Because  $E_D$  and  $R_D$  were assumed as constant values while effects of diffusion leakages could change direction according the gradient, only taking account for a single effect might lead to bigger measurement errors than without correction, suggesting that the appropriate method must be applied.

## Discussion

**Leakage coefficients of the empty chamber:** The equations for estimating  $K_W$  and  $K_C$  (Eqs. 1, 2) were developed for an empty chamber based on mass balance equations and the DGM for diffusions of a ternary gas mixture ( $\text{H}_2\text{O}$ ,  $\text{CO}_2$ , and dry air). The calculations of  $K_W$  and  $K_C$  are independent of each other due to approximations in the equation derivations, *i.e.*  $\text{CO}_2$  leakage and concentration are very small compared to the leakage and concentration of  $\text{H}_2\text{O}$  (or dry air), respectively. Eq. A14 is the same as suggested by the manufacturer (*Li-Cor* 2008). The manufacture's equation is based on Fick's law. As noted earlier, Fick's law is not theoretically correct for a ternary gas mixture and does not include Knudsen diffusion. As such, the leakage and measurement error correction equations in previous studies (*Li-Cor* 2008, Rodeghiero *et al.* 2007, Flexas *et al.* 2007) do not include the dry air component. In addition, there is no flow correction term needed in our expressions for determining  $K_W$  and  $K_C$  (Eqs. A15, A16), *i.e.*  $L_W$  and  $L_C$  do not alter the bulk flow rate though the leaf chamber since they are balanced by  $L_A$ . Rodeghiero *et al.* (2007) incorrectly adapted the equations of von Caemmerer and Farquhar (1981), used to describe  $\text{H}_2\text{O}$  and  $\text{CO}_2$  exchanges through a stoma with no dry air source/sink, to estimate  $K_W$  and  $K_C$ , and included a flow correction term. According to the authors, this resulted in *ca.* 2% higher values of  $K_W$ , while the effect of their flow correction on  $K_C$  estimates could be 20–60% for the chamber  $\text{CO}_2$  mole fractions ranging from  $1,200$ – $2,000 \mu\text{mol mol}^{-1}$ .

In the present study,  $K_C$  for the  $6 \text{ cm}^2$  and  $2 \text{ cm}^2$

chambers (Fig. 1C,D) of instrument-B with the worn gaskets were similar to the values of  $0.46$ ,  $0.40$ , and  $0.44 \mu\text{mol s}^{-1}$  from the *Li-6400* manual (*Li-Cor* 2008), Rodeghiero *et al.* (2007), and Flexas *et al.* (2007) respectively. However, it was greater than the value of *cca.*  $0.2 \mu\text{mol s}^{-1}$  estimated by McDermitt *et al.* (2001) and less than the results from instrument-A. The leakage of  $\text{H}_2\text{O}$  has been little considered (Rodeghiero *et al.* 2007). Water leakage is not only an issue in the transpiration measurement, but also a potential problem in calculations of  $K_C$  (Eq. 3),  $P_N$  (Eq. 5),  $g_s$  (Eq. 6) and  $C_i$  (Eq. 7), and, in fact,  $K_W$  was 8 to 10-fold greater than  $K_C$  (Fig. 1). Using the same equation, for the  $6 \text{ cm}^2$  chamber,  $K_W$  was much higher than the value  $0.89 \mu\text{mol s}^{-1}$  determined by Rodeghiero *et al.* (2007), and much lower than the value  $6.78 \mu\text{mol s}^{-1}$  for the  $2 \text{ cm}^2$  chamber or the value determined in the instrument-A.

Consistent linear relationships as indicated in Eq. 1 and Eq. 2 for  $K_W$  and  $K_C$  and Fig. 1 were also found in reinterpretation of the results from Flexas *et al.* (2007) for  $K_C$  and Rodeghiero *et al.* (2007) for both  $K_W$  and  $K_C$ . We concluded that the models of equations (1) or (2) are valid for estimating  $K_W$  and  $K_C$  for an empty chamber, and the different values of  $K_W$  and  $K_C$  in instruments A and B may reflect a difference in instrument conditions, such as leaf gasket tightness, gasket width and age, and condition of the O ring and back gasket seal. These results strongly suggested that  $K_W$  and  $K_C$  should be determined for each specific instrument (and chamber).

**Effect of presence of a leaf:**  $K_W$  and  $K_C$  of the chamber with a dead leaf (dried or thermally killed) were different from those of an empty chamber since the leakages between leaf and gasket are different from leakages between gaskets. Because both types of dead leaves can be a  $H_2O$  source/sink, the determination of  $K_W$  (Eq. 1) for a chamber filled with a dead leaf should be under the condition that leaf water is balanced with air inside the leaf chamber. When the dead leaf is placed into a new environment, a new water balance is established with the surrounding air, *i.e.* from a  $H_2O$  source/sink to a neutral conditions. At this stage,  $K_W$  can be obtained but the process for a dried or thermally killed leaf may take 20 min or longer (Fig. 2).

In the 2 cm<sup>2</sup> chamber,  $K_W$  for a dried potato or soybean leaf (Table 2) was much lower than the value of 5.11  $\mu\text{mol s}^{-1}$  estimated by Rodeghiero *et al.* (2007) for a dead *Quercus ilex* leaf, while in 6 cm<sup>2</sup> chamber, the average value of  $K_W$  was similar in comparison with the value 1.86  $\mu\text{mol s}^{-1}$  of Rodeghiero *et al.* (2007). While the present study observed small  $K_W$  values regardless of chamber size (Table 2), Rodeghiero *et al.* (2007), showed a larger difference between two sized chambers. They explained the reason was partly due to effects of water vapor sorption and desorption by the dried leaf for the  $K_W$  determination. Indeed, their leaf chamber was moister than the outside air, as a result their  $K_W$  would be larger than that at water balance state (Fig. 2A), and a small chamber usually needs a longer time period to reach a steady state (Li-Cor 2008). The relative large variations of  $K_W$  might reflect the more sensitive response of  $K_W$  to the different structure of the dead leaves.

The determination of  $K_C$  using a dried leaf was recommended by Long and Bernacchi (2003), and analyzed by Rodeghiero (2007) with *Quercus ilex* L. leaves; however, Flexas *et al.* (2007) argued that characteristics of a thermally killed leaf more closely resembled those of a living leaf. Our equation for determining  $K_C$  (Eq. 3) with a thermally killed leaf differed from the method of Flexas *et al.* (2007) and Alonso *et al.* (2009). Eq. 3 can be rearranged as:

$$P_{NA} = \frac{S K_C}{100} C_s + \left[ \frac{K_W (W_s - W_a) C_s}{100 S (1000 - W_s)} - \frac{S K_C C_a}{100} \right] \quad (8)$$

To obtain the linear relationship between  $P_{NA}$  and  $C_s$  based on the slope of  $S K_C/100$ , the authors were restricted to the special case where the second term was small [*i.e.* ( $W_s - W_a$ )  $C_s$  is small] and  $C_a$  was constant (Flexas *et al.* 2007, Alonso *et al.* 2009). These conditions are restricted to conditions with small water vapor leakage and stable values of ambient  $CO_2$  concentration, whereas such restrictions do not apply for Eq. 3 in the current study. Our method also differed from Rodeghiero *et al.* (2007) who determined  $K_C$  with a dried leaf using a variation of Eq. A22a when  $E_A$  is very small. The authors obtained  $K_C$  as the slope of the linear relationship

in  $\frac{100 (C_s - C_r)}{C_a - C_s}$  vs.  $1/F_i$ , but only when  $C_r$  is small (Rodeghiero *et al.* 2007 used a value of 50  $\mu\text{mol mol}^{-1}$ ). The significant linear regressions of  $100 P_{NA} S - \frac{K_W (W_s - W_a) C_s}{1000 - W_s}$  vs.  $C_a - C_s$  in our experiments (Table 2), and of  $P_{NA}$  vs.  $C_s$  in Alonso *et al.* (2009) and Flexas *et al.* (2007) suggest estimates for  $K_C$  with thermally killed leaves were correct, and variation in  $K_C$  values with different leaves were presumably due to differences in leaf structure.

$K_C$  measured by instrument-B in the 2 cm<sup>2</sup> chamber with a thermally killed leaf was similar to the empty chamber, but larger than that with a tobacco leaf (Flexas *et al.* 2007), and a spring wheat leaf (Alonso *et al.* 2009) (using a different gas analyzer: CIRAS-2, PP System, Hitchin, Hrttyd, UK with a 1.7 cm<sup>2</sup> chamber). The 2 cm<sup>2</sup> instrument-B  $K_C$  value was also lower than the one estimated in instrument-A and -B fitted with the 6 cm<sup>2</sup> chamber. Overall, such comparisons along with the results in Table 2 indicated that the equation we developed was reliable. Observed differences in  $K_C$  for leaves from different plant species could be explained as a result of different leaf structures and instrument bias. As  $K_C$  within a given instrument and chamber size varied with leaf condition (dried or thermally killed) and whether or not the chamber was empty, we suggest that  $K_C$  be determined with a thermally killed leaf to correct for measurement errors, in light of the fact that the leaf structure is most similar to a living leaf (Flexas *et al.*, 2007). The lower  $K_C$  for new versus worn gaskets (0.56 vs. 0.89  $\mu\text{mol s}^{-1}$ ) contrasted with Rodeghiero *et al.* (2007), who found  $K_C$  for worn gaskets was 20–30% lower than the  $K_C$  for new gaskets. This difference further suggests that  $K_C$  be determined, and the correction be made, under similar gasket conditions to decrease correction errors due to different gasket conditions.

**The correction of measurement error:** According to Eq. 4 and Eq. 5, any method that can (1) reduce  $H_2O$  and  $CO_2$  mole fraction gradients between inside and outside chamber will decrease leakage errors, (2) decrease permeability for  $CO_2$  and  $H_2O$  between gasket and leaf can also decrease the leakage errors since the major leakages are between gasket and leaf rather than the gasket itself, and (3) increase the chamber window area and/or reduce the gasket area can reduce leakage and dark transpiration and respiration errors. However, in practice, one method may be offset by another, *i.e.* reducing the gasket area to decrease the inward gas exchange released from the leaf portion under the gasket may increase the permeability or *vice versa*. Several methods to minimize leakage of  $CO_2$  were tested by Flexas *et al.* (2007), but leakage of  $H_2O$ , and inward  $E_D$  and  $R_D$  released from the leaf under the gasket were not considered. They argued that methods to reduce chamber leakage did not seem promising for correcting measurements. Rodeghiero *et al.*

(2007) suggested using a double gasket design to reduce the diffusion leakages, thereby diminishing gas gradients. In the present study, since both  $K_C$  and  $K_W$  were easy to estimate and the values were very stable for a specific leaf and instrument, we strongly recommend that measurement errors be corrected by using  $K_C$  and  $K_W$ , and  $E_D$  and  $R_D$  under the specific experimental conditions desired by the user.

Flexas *et al.* (2007) and Alonso *et al.* (2009) corrected net  $\text{CO}_2$  exchange rate by simple subtraction of the relationship between  $C_s$  and  $P_{NA}$  of a chamber filled with a dead leaf. Alonso *et al.* (2009) suggested that  $\text{H}_2\text{O}$  diffusion was too small to need to correct for. As indicated in Eq. 8, their method is a good approximation for correcting  $P_{NA}$ , but only if the effect of dark respiration from the leaf under the gasket can be ignored and the same values of  $(W_s - W_a)$   $C_s$  and ambient  $\text{CO}_2$  are maintained when determining the  $\text{CO}_2$  leakage and measuring  $P_N$  for a living leaf (Eqs. 5, 8). The correction methods for  $P_N$  suggested by Rodeghiero *et al.* (2007) and the manufacture (Li-Cor 2008) also did not include both effects of  $R_D$  and  $\text{H}_2\text{O}$  leakage. The method provided by Pons and Welschen (2002) only considered the measurement error due to respiration under the gasket (see also Lenz *et al.* 2010). The correction method for  $E$  suggested by Rodeghiero *et al.* (2007) simply added the  $\text{H}_2\text{O}$  leakage and did not correct for the correction of flow rate, which is typically a 3% error; it also did not account for the dark transpiration from the leaf under the gasket. Our suggested approaches address these limitations.

#### Effects on parameterization of model of Farquhar:

The parameterization of the Farquhar *et al.* (1980) biochemical model for a  $\text{C}_3$  leaf was based on  $P_N/C_i$  curves using methodology in Sharkey *et al.* (2007).  $C_i$  was calculated by Eq. 7a for potato, or by Eq. 7b for the

soybean leaf. Thus, effects of all measurement errors involved in correcting  $P_N$  and  $C_i$  on the parameterization were evaluated. Note the results in Fig. 3 and Table 3 were examples for specific potato and soybean leaves under specific conditions, *i.e.* the range of water vapor gradient was typically between  $-15$  to  $+15$   $\text{mmol mol}^{-1}$  and it was assumed constant values of the  $R_D$  and  $E_D$ . If experimental conditions change, the magnitude of the effects of measurement errors will alter accordingly.

The effects of diffusion leakages on  $C_i$  are mainly dependent on the correction of  $P_N$  due to  $L_C$  (Eqs. 7a, 7b). For example, for the  $P_N/C_i$  measurement using the  $2$   $\text{cm}^2$  chamber for the potato leaf, at a  $C_s$  of  $1,963$   $\mu\text{mol mol}^{-1}$  and water vapor gradient of  $8.2$   $\text{mmol mol}^{-1}$ , the  $C_i$  was underestimated by  $28$   $\mu\text{mol mol}^{-1}$  if only considering  $L_W$ . However,  $C_i$  would be underestimated by  $109$   $\mu\text{mol mol}^{-1}$  if  $L_C$  was included. The effect of  $L_W$  was less important than the effect of  $L_C$ , but was significant. This contrasts with the conclusion that  $\text{H}_2\text{O}$  diffusion leakages influence  $P_N/C_i$  curves at least as much as  $\text{CO}_2$  diffusion leaks (Rodeghiero *et al.* 2007).

Fig. 3 and Table 3 show effects of correcting for different measurement errors on the  $P_N/C_i$  curves and model parameters. The significant differences between corrections for all experimental errors as opposed to only diffusive leakages and inward  $R_D$  and  $E_D$  suggest that correcting for only a portion of these errors might be worse than making no corrections at all since the magnitude and direction of  $L_W$  and  $L_C$  change according to their gradients, while the direction and effects of inward  $R_D$  and  $E_D$  from under gasket do not change. All previous studies only corrected for a portion of the measurement errors, such as the error due to  $R_D$  under the gasket (Pons and Welschen 2002, Lenz *et al.* 2010), only the  $\text{CO}_2$  leakage (*e.g.*, Flexas *et al.* 2007), or only  $\text{H}_2\text{O}$  and  $\text{CO}_2$  leakages (*e.g.*, Rodeghiero *et al.* 2007).

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## Appendix: Detailed Equation Derivations

### (I) Diffusive leakage coefficients of an empty chamber

At steady-state condition, the mass balance equations for H<sub>2</sub>O and CO<sub>2</sub> with diffusion leakages into an empty chamber can be expressed as

$$\frac{F_o W_s - F_i W_r}{10^6} = L_W \quad (A1)$$

and

$$\frac{F_o C_s - F_i C_r}{10^6} = L_C \quad (A2)$$

where  $F_i$  and  $F_o$  are the incoming and outgoing air flow rate, respectively;  $W_s$  and  $W_r$  are the sample and reference water vapor mole fraction,  $C_r$  and  $C_s$  are the sample and reference CO<sub>2</sub> mole fraction;  $L_W$  and  $L_C$  are the water and CO<sub>2</sub> leakage rate.

At steady-state condition, the air mixture pressure in an empty chamber keeps constant. Based on Dalton's law and the ideal gas law, the total air mixture pressure in the leaf chamber can be expressed as

$$P_{am} V = (n_{CO_2} + n_{H_2O} + n_{da}) R T \quad (A3)$$

where  $P_{am}$  is the pressure of the air mixture inside the chamber;  $V$  is the volume of the chamber,  $R$  is the universal gas constant,  $T$  is the temperature of the leaf chamber; and the  $n_{CO_2}$ ,  $n_{H_2O}$  and  $n_{da}$  are the number of moles of CO<sub>2</sub>, of H<sub>2</sub>O and dry air respectively. Because  $V$ ,  $R$  and  $T$  keep constant, the total number of moles of  $n_{CO_2}$ ,  $n_{H_2O}$  and  $n_{da}$  must be a constant. Therefore, the total leakages of CO<sub>2</sub>, H<sub>2</sub>O and dry air ( $L_W$ ) is equal to zero.

$$L_C + L_W + L_A = 0 \quad (A4)$$

Because of the H<sub>2</sub>O, CO<sub>2</sub> diffusive leakages,  $W_s \neq W_r$  and  $C_s \neq C_r$  in Eq. A1 and Eq. A2; however, since the sum of leakages of H<sub>2</sub>O, CO<sub>2</sub> and dry air is zero (Eq. A4),  $F_o = F_i$ . Eq. A1 and Eq. A2 can be simplified

$$L_W = \frac{F_i (W_s - W_r)}{10^6} \quad (A5)$$

and

$$L_C = \frac{F_i (C_s - C_r)}{10^6} \quad (A6)$$

The air mixture can be treated as ternary system with H<sub>2</sub>O, CO<sub>2</sub> and dry air (Jarman 1974, von Gaemmerer and Farquhar 1981, Leuning 1983). The DGM (Mason and Malinauskas 1983) can describe the leakages of H<sub>2</sub>O and CO<sub>2</sub> through the leaf chamber. Ignoring both thermal and baric diffusions, which are typically small, the H<sub>2</sub>O and CO<sub>2</sub> leakages can be approximately obtained by

$$\frac{\Delta W}{10^6 \Delta l} = -\frac{\overline{A_{as}} L_W - \overline{W_{as}} L_A}{S C_{AM} D_{wa}} - \frac{\overline{C_{as}} L_W - \overline{W_{as}} L_C}{1000 S C_{AM} D_{cw}} - \frac{L_W}{S C_{AM} D_W^k} \quad (A7)$$

and

$$\frac{\Delta C}{10^6 \Delta l} = -\frac{\overline{A_{as}} L_C - \overline{C_{as}} L_A}{S C_{AM} D_{ac}} - \frac{\overline{W_{as}} L_C - \overline{C_{as}} L_W}{S C_{AM} D_{cw}} - \frac{L_C}{S C_{AM} D_C^k} \quad (A8)$$

where W and C are water and CO<sub>2</sub> concentrations, respectively;  $\Delta l$  is the diffusion effective length;  $D_{wa}$ ,  $D_{cw}$  and  $D_{ac}$  are the diffusivities for binary mixtures of H<sub>2</sub>O and dry air, CO<sub>2</sub> and H<sub>2</sub>O, and air and CO<sub>2</sub>, respectively;  $D_W^k$  and  $D_C^k$  are the Knudsen diffusivities for H<sub>2</sub>O and CO<sub>2</sub>, respectively;  $C_{AM}$  is the total air mixture concentration, which is assumed as a constant; S is the area of the chamber window;  $\overline{A_{as}}$ ,  $\overline{W_{as}}$  and  $\overline{C_{as}}$  are the mean molar fractions of dry air, H<sub>2</sub>O and CO<sub>2</sub> along the leaf chamber, respectively, *i.e.*  $\overline{W_{as}} = (W_a + W_s)/2$ ,  $\overline{C_{as}} = (C_a + C_s)/2$ , and subscripts a and s indicate ambient and inside leaf chamber, respectively. The first four terms in Eq. A7 and Eq. A8 are due to the collisions of molecules and are based on the Stefan-Maxwell equation. The fifth terms are due to the collisions between gas molecules and pore walls.

Since  $D_{ac} \approx D_{cw}$ ,  $D_{wa} \approx 1.6 D_{cw}$ , the CO<sub>2</sub> mole fraction is a small part of the total gas mixture ( $\overline{C_{as}}/10^3 \leq \overline{A_{as}} + \overline{W_{as}}$ ) and CO<sub>2</sub> diffusive leakage rate is small compared to the diffusive leakage of H<sub>2</sub>O and dry air ( $L_C/10^3 \ll L_W$ );  $\frac{\overline{A_{as}}}{10^3} + \frac{\overline{W_{as}}}{10^3} + \frac{1.6 \overline{C_{as}}}{10^6} \approx \frac{\overline{A_{as}}}{10^3} + \frac{\overline{W_{as}}}{10^3} \approx 1$ ,  $L_C + L_W = -L_A \approx L_W$  and the fourth term in Eq. A7 is negligible. We obtain

$$\frac{\Delta W}{10^6 \Delta l} = -\left(\frac{1}{S C_{AM} D_{wa}} + \frac{1}{S C_{AM} D_W^k}\right) L_W \quad (A9)$$

and

$$\frac{\Delta C}{10^6 \Delta l} = -\left(\frac{1}{S C_{AM} D_{ac}} + \frac{1}{S C_{AM} D_C^k}\right) L_C \quad (A10)$$

The diffusive leakage coefficients of H<sub>2</sub>O in the air ( $K_W$ ) and CO<sub>2</sub> in air ( $K_C$ ) are defined as

$$\frac{1}{K_W} = \frac{\Delta l}{S C_{AM}} \left( \frac{1}{D_{wa}} + \frac{1}{D_W^k} \right) \quad (A11)$$

and

$$\frac{1}{K_C} = \frac{\Delta l}{S C_{AM}} \left( \frac{1}{D_{ca}} + \frac{1}{D_C^k} \right) \quad (A12)$$

Eq. A9 and Eq. A10 can be simplified to

$$\frac{W_s - W_a}{10^6} = \frac{L_W}{K_W} \quad (A13)$$

and

$$\frac{C_a - C_s}{10^6} = -\frac{L_C}{K_C} \quad (A14)$$

Eq. A13 and Eq. 14 have the same form as Fick's law, but they are derived from the DGM under the conditions noted above. Combining Eq. A5 and Eq. A13, Eq. A6 and Eq. A14, respectively; we can obtain the working equations for  $K_W$  and  $K_C$  as

$$K_W = \frac{F_i (W_s - W_r)}{(W_a - W_s)} \quad (A15)$$

and

$$K_C = \frac{F_i (C_r - C_s)}{(C_s - C_a)} \quad (A16)$$

Note that Eq. A15 is different from Eq. 3 of Rodeghiero *et al.* (2007). There is no flow rate correction in Eq. A15 for an empty chamber. Eq. A16 is different from Eq. 6 of Rodeghiero *et al.* (2007). Leakage of H<sub>2</sub>O does not affect K<sub>C</sub> for an empty chamber.

## (2) Leakage coefficients of the chamber with a dead leaf

The K<sub>W</sub> and K<sub>C</sub> might be significantly different when a living leaf is enclosed in the chamber vs. an empty chamber because the leakage between gasket and leaf may be different from the leakage between gaskets. The leakage coefficients should be determined under experimental conditions with as close to a real living leaf as possible. As suggested by Flexas *et al.* (2007), a thermally killed leaf, or a dried leaf as used by Long and Bernacchi (2003) could be considered as a substitute for a living leaf for this purpose. However, because the dead leaf can be a source/sink of H<sub>2</sub>O, the K<sub>W</sub> cannot be determined directly by Eq. A15, and the K<sub>C</sub> cannot be calculated using Eq. A16. At steady state, the net flux of a gas can be closely approximated by the sum of independent contributions of diffusive flow. When there is a leaf inside a chamber, mass balance for H<sub>2</sub>O can be expressed as

$$\frac{F_o W_s - F_i W_r}{10^6} = 10^{-4} S E - L_W + 10^{-4} S D_W \quad (\text{A17})$$

where D<sub>W</sub> is the evaporation escape from the leaf under gasket. The mass balance of gas mixture is given as (ignoring the change in CO<sub>2</sub>)

$$F_o = F_i + 0.1 S E - 1000 L_W - 1000 L_A + 0.1 S D_W \quad (\text{A18})$$

Since  $L_W \approx -L_A$  (Eq. A4), Eq. A18 can be simplified to

$$F_o = F_i + 0.1 S E + 0.1 S D_W \quad (\text{A19})$$

Substituting Eq. A19 into Eq. A17,

$$E = \frac{10 F_i (W_s - W_r)}{S (1000 - W_s)} + \frac{10^7 L_W}{S (1000 - W_s)} - D_W \quad (\text{A20a})$$

The first term of Eq. A20a is the apparent transpiration rate ( $E_A$ ). The second term is the influence of  $L_W$  modified by the effect of H<sub>2</sub>O dilution inside the chamber. Substituting Eq. A13 to Eq. A20a, we have

$$E = E_A + \frac{10 K_W (W_s - W_a)}{S (1000 - W_s)} - D_W \quad (\text{A20b})$$

If water from the dead leaf evaporates, it is not possible to determine  $E$  prior to determination of K<sub>W</sub>. However, if  $W_r$  keeps stable, the water vapor of dead leaf will be eventually balanced with  $W_s$ , *i.e.*,  $E = 0 = D_W$ . Under these conditions, Eq. A20 becomes Eq. A15. Note that estimating K<sub>W</sub> in the chamber with a dead leaf requires two conditions: one is steady state and another  $E = D_W = 0$ . When approaching this point, the thermally killed leaf becomes a dried leaf. A very dried leaf may become a little wet by absorbing water vapor from its environment. Therefore, K<sub>W</sub> estimated from a dead leaf (thermally killed leaf or dried leaf) represents its value when the dead leaf balanced with its environment. The working equation for leakage coefficient of water vapor has the same form as for an empty chamber (Eq. A15).

Since there is no CO<sub>2</sub> source/sink inside the chamber filled with a dead leaf, the mass balance of CO<sub>2</sub> can be given by Eq. A2. Substituting Eq. A19 into Eq. A2, we obtain

$$\frac{F_i (C_r - C_s)}{100 S} - \frac{C_s (E + D_W)}{1000} = \frac{L_C}{10^{-4} S} \quad (\text{A21})$$

Substituting Eq. A20b into Eq. A21,

$$\frac{F_i (C_r - C_s)}{100 S} - \frac{E_A C_s}{1000} - \frac{K_W (W_s - W_a) C_s}{100 S (1000 - W_s)} = \frac{L_C}{10^{-4} S} \quad (\text{A22a})$$

The first two terms of Eq. A22a is the  $P_{NA}$ . The third term is the influence of H<sub>2</sub>O leakage. Eq. A22a becomes,

$$P_{NA} - \frac{K_W (W_s - W_a) C_s}{100 S (1000 - W_s)} = \frac{K_C (C_s - C_a)}{100 S} \quad (\text{A22b})$$

Eq. A22b can be rearranged as

$$K_C = \frac{100 P_{NA} S - \frac{K_W (W_s - W_a) C_s}{1000 - W_s}}{C_s - C_a} \quad (\text{A23a})$$



Note that Eq. A23a is different from Eq. 6 of Rodeghiero *et al.* (2007). It also includes the effect of leaf evaporation (in  $P_{NA}$ ). When the second term can be negligible compared to the first term (*e.g.* when  $W_a$  is close to  $W_s$  and/or  $C_s$  is very small), Eq. A23a can be simplified as

$$K_C = \frac{100 P_{NA} S}{C_s - C_a} \quad (A23b)$$

(3) Inward gas exchanges and correction for the measurement errors for gas leakages

When the leaf chamber clamps onto a leaf to measure  $P_N$  and  $E$ ,  $D_E$  and  $D_C$  released by the dark transpiration ( $E_D$ ) and respiration ( $R_D$ ) from the leaf under gasket will enter into the interior of the leaf chamber, leading to a higher  $E_A$  and a lower  $P_{NA}$ .  $D_C$  can be estimated by (Pons and Welschen 2002, Lenz *et al.* 2010)

$$D_C = r R_D \quad (A24)$$

Since  $H_2O$  and  $CO_2$  exchanges share the same pathway,  $D_W$  is determined by

$$D_W = r R_W \quad (A25)$$

where  $r$  is the ratio of the gasket area of the inward portion to the chamber window area (Pons and Welschen 2002, Shapiro *et al.* 2004, Lenz *et al.* 2010) for homobaric leaves with high resistance to lateral gaseous transport and heterobaric leaves. The ratios of two chambers used in this study are listed in Table 4. The  $E_D$  and  $R_D$  can be obtained by

$$E_D = \frac{E_{DA} + \frac{10 K_W (W_s - W_a)}{S (1000 - W_s)} C_s}{1 + r} \quad (A26)$$

and

$$R_D = \frac{R_{DA} + \frac{K_W (W_s - W_a) C_s}{100 S (1000 - W_s)} - \frac{K_C (C_a - C_s)}{100 S}}{1 + r} \quad (A27)$$

At steady state, when there is a living leaf inside a chamber, mass balance for  $H_2O$  flux and for mixture gas can be expressed as Eq. A17 and Eq. A19, respectively. The working equation for the correction of transpiration is

$$E = E_A + \frac{10 K_W (W_s - W_a)}{S (1000 - W_s)} - r E_D \quad (A28)$$

Note that Eq. A28 is different from the Eq. 10 of Rodeghiero *et al.* (2007). The effect of leakage of  $H_2O$  is adjusted by flow rate change. The mass balance of  $CO_2$  can be given by

$$\frac{F_o C_s - F_i C_r}{1000} = -10^{-4} S P_N - L_C - 10^{-4} S D_C \quad (A29)$$

Table 4. The dimensions of two standard leaf chambers of *Li-6400*.

| Chamber model                              | 6400-2B | 6400-40 |
|--|---------|---------|
| Window area [cm <sup>2</sup> ]             | 6.00    | 2.00    |
| Gasket area [cm <sup>2</sup> ]             | 7.44    | 4.14    |
| Gasket width [cm]                          | 0.60    | 0.60    |
| Gasket inward part [cm <sup>2</sup> ]      | 3.31    | 1.79    |
| Ratio of gasket inward part to window area | 0.55    | 0.89    |

Substituting Eq. A19 into Eq. A29, we obtain,

$$P_N = \frac{F_i (C_r - C_s)}{100 S} - \frac{E C_s - D_W C_s}{1000} - \frac{L_C}{10^{-4} S} - D_C \quad (A30)$$

Substituting Eq. A20b and Eq. A24 into Eq. A30,

$$P_N = P_{NA} - \frac{K_W (W_s - W_a) C_s}{100 S (1000 - W_s)} + \frac{K_C (C_a - C_s)}{100 S} - r R_D \quad (A31a)$$

Note that Eq. A31a is different from Eq. 13 of Rodeghiero *et al.* (2007). It takes effects of adjusted  $L_W C_s$  and inward respiration into account. When  $W_s$  is close to  $W_a$  or  $C_s$  is very small, Eq. A31a is simplified to

$$P_N = P_{NA} + \frac{K_C (C_a - C_s)}{100 S} + D_C \quad (\text{A31b})$$

(4) The measurement protocol:

Carefully select at least 3 leaves with similar structure to living leaves that will be measured. The leaves are killed by immersion in boiling water until no variable chlorophyll fluorescence is detectable as measured by a chlorophyll meter. The thermally killed leaf is then blotted and enclosed in the chamber of a ready to be used open gas-exchange system.

$K_C$  is determined by performing  $P_{NA}/C_i$  curves at  $C_a$  of 50, 200, 1,500; and 2,000  $\mu\text{mol mol}^{-1}$  using Eq. 3. The measurements will be completed before the leaf is dry.

$K_W$  is determined when  $E_A$  is stable by Eq. 1. A low negative water vapor gradient (lower than 10  $\text{mmol mol}^{-1}$ ) between inside and outside the leaf chamber can be achieved by adjusting the valve of the desiccant tube to decrease the water vapor mole fraction inside the chamber. A large positive water vapor gradient (larger than 10  $\text{mmol mol}^{-1}$ ) can be achieved by adding a few drops of distilled water to the soda lime tube to increase water vapor mole fraction inside the chamber.

Dark transpiration is determined by Eq. A26 and dark respiration by Eq. A27. At least 3 leaves with similar structure and age to living leaves will be measured are selected.

Correction of measurement errors by Eq. 4 and Eq. 5 and calculation  $g_s$  and  $C_i$  by Eq. 6 and Eq. 7. The ambient mole fractions of  $\text{CO}_2$  and  $\text{H}_2\text{O}$  should be recorded. In practice, there may not be  $\text{CO}_2$  and  $\text{H}_2\text{O}$  sensors available to monitor  $C_a$  and  $W_a$ . Ambient  $\text{CO}_2$  and  $\text{H}_2\text{O}$  can be obtained by the same open gas exchange system before and after each measurement or each  $P_N/C_i$  curve.